

Evaluation of edge cracks in cross-ply laminates using image correlation and thermoelastic stress analysis

G.P. Battams^a, J.M. Dulieu-Barton^b and S.W. Boyd^c

School of Engineering Sciences, University of Southampton, Southampton, SO17 1BJ, UK

^aG.Battams@soton.ac.uk, ^bjanice@soton.ac.uk, ^cS.W.Boyd@soton.ac.uk

Keywords: Edge cracks, cross ply polymer composite laminate, notched, GFRP, TSA, DIC, thermoelastic stress analysis (TSA), digital image correlation (DIC).

Abstract. The paper describes initial work on using 2D digital image correlation (DIC) and thermoelastic stress analysis (TSA) to obtain data from edge cracks in cross-ply laminates. It is demonstrated that detailed data related to the crack tip stresses can be obtained using TSA. The work reveals some of the limitations experienced when using DIC in applications where high spatial resolution is required. A detailed discussion is provided along with an outline for future work.

Introduction

The increasing use of composites in many crucial engineering applications has placed greater demand on techniques to assess stress concentrations. Damage accumulation in metals is often localised to cracks and can be predicted using various fracture mechanics approaches [1]. In comparison, laminated polymer composite materials display many forms of damage which interact with each another during initiation and propagation. The mechanisms are also dependent on the constituent material and laminate stacking sequence. Matrix cracking is prominent in 90° layers when loaded in tension and occurs well below the failure load of the laminate [2]. Such cracking has a relatively small affect on the stiffness of a structure but does initiate other types of damage such as fibre breakage and delamination. Therefore it is necessary to apply experimental techniques to provide enhanced understanding of the failure mechanisms

Strain measurements using strain gauges or extensometers are useful for obtaining point readings but only provide information at discrete points. Therefore, for complex components full field techniques are more applicable, especially for identification of damage initiation. Two full field techniques that are commonly used are Digital Image Correlation (DIC) and Thermoelastic Stress Analysis (TSA). TSA has been used in relatively few studies on notched or cracked polymer composite specimens [3, 4]. Optical techniques have been used extensively in many materials including metals, ceramics and composites [5]. However, TSA and DIC have not been used in conjunction to obtain data relating to the stress and strain in the component. In the present paper the two techniques will be used to examine the stress/strain distribution produced around an edge notch in a composite specimen. The edge notch provides challenges for both techniques in terms of spatial and temporal resolution. The purpose of the paper is to apply the TSA and DIC techniques to an edge notch in a polymer composite component and to identify the advantages and limitations of using each technique in this application. The motivation is to establish a means of assessing the failure mechanisms at the notch. The failure occurs rapidly and therefore a high speed camera is used with the DIC. It is shown that the TSA provides an excellent validation tool for the DIC.

Experimental Techniques

TSA is a well established technique for providing full-field stress data for orthotropic composite materials [3, 4]. The underlying theory is presented in the review [3]. For an orthotropic material such as a laminated polymer composite the temperature change, ΔT , is related to the change in stress as follows [4]:

$$\Delta T = -\frac{T}{\rho C_p}(\alpha_1 \Delta \sigma_1 + \alpha_2 \Delta \sigma_2) \quad (1)$$

where C_p is the specific heat at constant pressure, T is the absolute temperature on the surface, α denotes the coefficient of thermal expansion and σ is the direct stress. The subscripts 1 and 2 denote the principal material directions.

The infra-red system used in this work is the Silver 480M manufactured by Cedip and has a maximum frame rate of 383 Hz at the full resolution of 320 x 256 pixels. The system is radiometrically calibrated and can deliver values of ΔT directly. In the present work the data will be presented in the form of $\Delta T/T$ to enable data to be compared to other data taken at different room temperatures and also to eliminate the effect of any localised heating close to the damage site. The measured data is T , with ΔT values obtained through performing TSA. This uses the lock-in function, requiring a load reference signal from the test machine used to load the specimens.

Digital Image correlation (DIC) is a technique that utilises standard white light cameras and the contrast of the specimen surface. The correlation was conducted using proprietary software: DaVis by LA Vision. Their correlation algorithm divides the imaged area into a grid of interrogation cells and tracks the movement of each cell in the images collected as a structural test progresses. To enable correlation between the cells, a random surface pattern must be used that has well contrasting pixel grayscale levels; this is achieved using spray paint. The images from the deformed and reference states are correlated, and the displacements obtained. Subsequently the strains are obtained by taking the displacement at the centre of the cell and differentiating over a gauge length defined by the distance between the centres of two adjacent cells. In this paper a single high speed Redlake Motionpro X-3 plus digital camera is used to obtain in-plane 2D deformations and strains. The camera has a maximum frame rate of 2000 Hz at a resolution of 1280 x 1024; higher rates can be achieved if the number of vertical pixels is reduced. The camera stores data internally and has a maximum storage size of 8 GB. The data collection is therefore a compromise between frame-rate, spatial resolution and available recording time.

Specimen manufacture and initial tests

A [90, 0, 90, 0]_s sheet of material was produced using Primco UD001/00 unidirectional glass-epoxy pre-impregnated material. The laminate was cured using an autoclave with an applied pressure of 4 bar at 125 °C for one hour. The cured laminate had an approximate thickness of 2 mm. Specimens were cut parallel and perpendicular to the 0° ply to give specimens with 90° and 0° surface layers respectively to specimens of 300 mm long by 25 mm wide. Edge notches were created with a fine piercing saw blade at the centre of the gauge length. The notches have an approximate width of 0.25 mm.

Initial tests were carried out to determine the approximate failure load and extension to failure of the specimens. Unnotched specimens were found to fail at 18.5 kN with 5.53 mm extension, giving a Ultimate Tensile Strength (UTS) of 388 MPa. When a notch of 2 mm was introduced into one side

of the specimen, the approximate failure load was found to be 13.0 kN at 3.35 mm extension, giving a critical stress intensity factor of around $34 \text{ MPa}/\text{mm}^{1/2}$ [1].

Tests were conducted at a ramp rate of $3.33 \times 10^{-3} \text{ m/s}$ on an Instron 5500 servo-mechanical test machine. During the ramp, white light digital images were collected using the Redlake Motionpro X-3 plus high speed digital camera at a frame rate of 7000/sec. The crack propagated across the width of the specimen in less than a second. Therefore a slower crack growth rate is required if the failure were to be imaged successfully. Decreasing the ramp rate to 0.1 mm/min slowed the crack propagation, but not enough for a fully controlled crack growth. The crack did not grow until the critical stress was achieved and then the crack grew rapidly, increasing in length by 2.5 mm in 0.25 s. Ideally, in the 2D DIC conducted here, the camera would image the deformations at a slower frequency during the initial part of the test to conserve memory and then operate at a higher frequency when the actual failure occurs. However, this camera cannot change frame rate mid test. Furthermore, calculations showed that a wider specimen would be necessary to achieve stable crack growth. It was considered that it is the strain field that occurs prior to crack initiation that is important. Therefore it was decided to concentrate on the imaging of the stress and strain fields of the notched specimens prior to failure rather than during crack growth in the experiments described in this paper.

Thermoelastic stress analysis

A cyclic load of 2 kN with a frequency 10 Hz was applied to both specimen types, i.e. one with a 90° surface ply and the other with a 0° surface, using an Instron servo-hydraulic test machine. During the tests, mean loads of 2, 3, 4, 6 and 10 kN were used to increase the load level in the specimen to initiate failure whilst keeping the background thermoelastic response at the same level. 1080 consecutive infra-red images were taken using a frame rate of 101 Hz with an integration time of $1300 \mu\text{s}$. The data were processed so that $\Delta T/T$ was obtained. These are shown in Figure 1 for the 0° surface ply in and Figure 2 for the 90° surface ply.

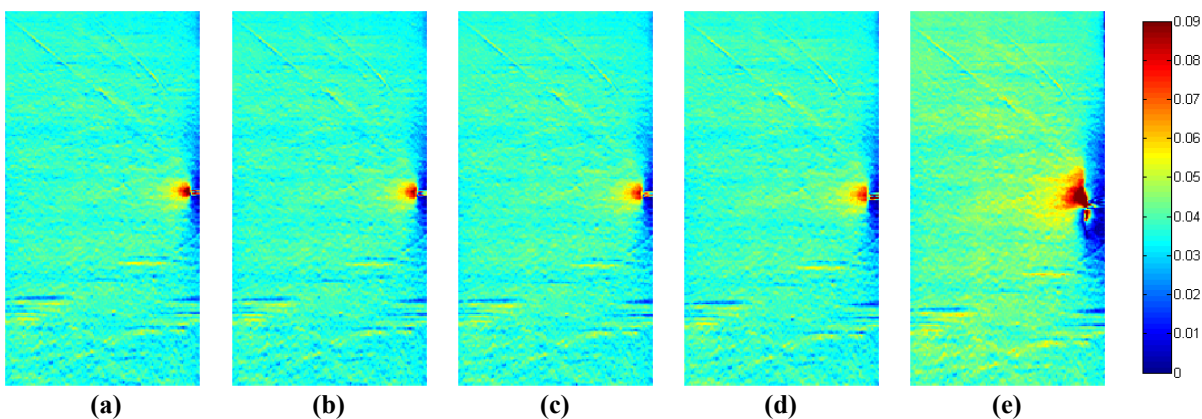


Figure 1: $\Delta T/T$ for increasing mean load for a 0° surface ply specimen (a) 2kN mean load (b) 3 kN mean load (c) 4 kN mean load (d) 6 kN mean load (e) 10 kN mean load (Image area = 1184 mm^2)

The average $\Delta T/T$ values away from the notch are $0.0375 \pm 0.0035 \text{ K}$ in Figure 1a and $0.0311 \pm 0.0035 \text{ K}$ in Figure 2a. This shows that the response of the surface ply for the same given applied stress is different corresponding to the findings of [4]. As the mean load increases there is little difference in the average $\Delta T/T$ readings for the 0° surface ply i.e. $0.0377 \pm 0.0034 \text{ K}$ for the 3 kN load, $0.0382 \pm 0.0034 \text{ K}$ for 4 kN, $0.0386 \pm 0.0035 \text{ K}$ for 6 kN and $0.0420 \pm 0.0036 \text{ K}$ at the 10 kN load. There is a steady increase in the average value indicating that there is an influence from the damage occurring in the sub surface 90° ply. This is supported by the readings from the 90° surface ply: $0.0314 \pm 0.0035 \text{ K}$ for 3 kN, $0.0339 \pm 0.0036 \text{ K}$ for 4 kN, 0.0322 ± 0.0035 for 6 kN and $0.0271 \pm 0.0037 \text{ K}$ for 10 kN. As damage evolves with increasing mean load, the 0° specimen experiences an

increase in thermoelastic response whereas for the 90° specimen the response reduces slightly and when gross damage occurs, reduces significantly. The explanation for this is simple; as the 90° plies fail at lower loads through the creation of transverse cracks, the load carrying capacity is transferred to the 0° plies and hence the response from one decreases and the other increases. The most interesting and revealing difference in the data is the indication of the presence of the notch. For the specimen with the 0° surface ply there is a clear stress concentration at the notch identified by an increasing $\Delta T/T$ value with the increasing mean load. This is very similar to what can be seen in an isotropic material with a crack e.g. [4]. In Figure 1e failure has started and there is a clear indication of longitudinal splitting emanating from the notch tip. For the 90° surface ply, the presence of the notch is indicated only by the reduction in the response above and below the notch where no load is carried. There is a slight increase in response but not at the notch tip. However there are clear indications of transverse cracking between the fibres particularly at the higher mean loads; Figure 2e shows that the transverse cracks have coalesced and the load carrying capability of the ply has diminished significantly. Figures 3 and 4 show plots along a horizontal line through the crack for both specimen types respectively. The peak in response is clearly shown in Figure 3 and is not apparent in Figure 4. There is a difficulty in that the strain in both these specimens is identical and yet the concentration at the crack-tip is not showing in one data set as the response is a result of the surface ply alone.

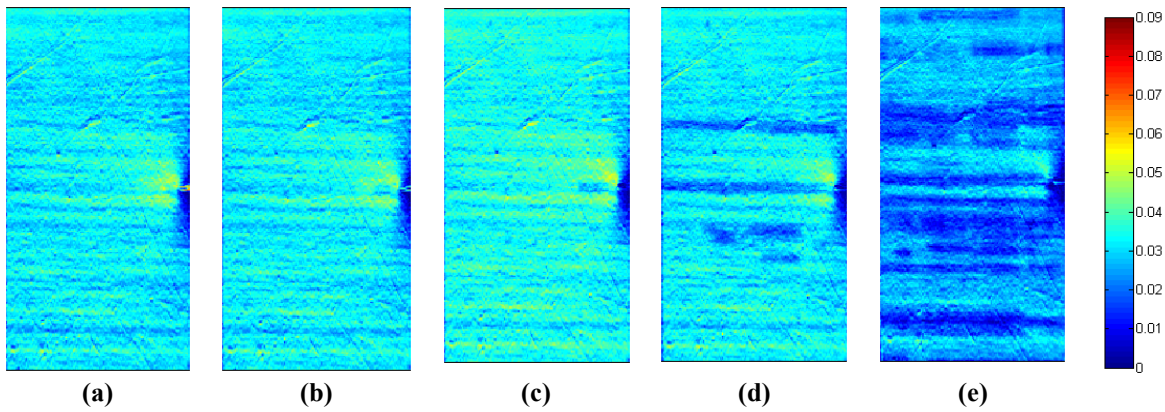


Figure 2: $\Delta T/T$ for increasing mean load for a 90° surface ply specimen (a) 2 kN mean load (b) 3 kN mean load (c) 4 kN mean load (d) 6 kN mean load (e) 10 kN mean load (Image area = 1115 mm²)

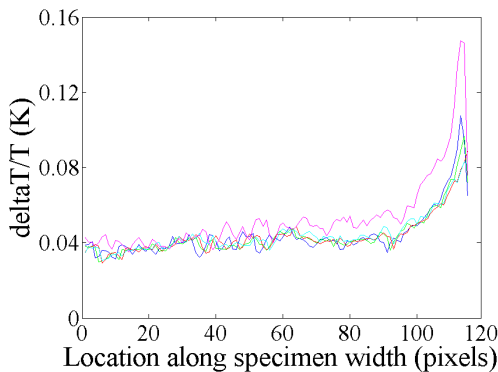


Figure 3: $\Delta T/T$ plot across specimen at notch with increasing mean load for a 0° surface ply specimen

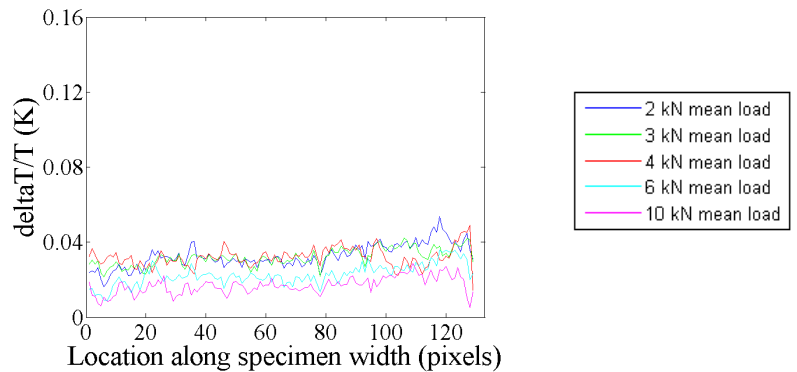


Figure 4: $\Delta T/T$ plot across specimen at notch with increasing mean load for a 90° surface ply specimen

Digital image correlation

0° and 90° surface ply specimens were tested quasi-statically to failure in an Instron 8802 servo-hydraulic test machine. Two ramp rates were used for the test to minimise overall test time and therefore maximise the image frame rate for the given camera storage capacity. Images were

captured during the initial ramp of 3.33×10^{-5} m/s up to a 3 mm deflection and the final ramp of 3.33×10^{-6} m/s to final failure. The camera was set to a frame rate of 30 Hz at a resolution of 1080 x 768 pixels giving a raw image spatial resolution of 0.024 mm. Two 1250 W tungsten lamps were used to illuminate the specimen; load data was simultaneously collected with each image. The speckle pattern was produced by spray paint and the quality of the image was found to be satisfactory based on a histogram of grayscale levels, with a contrast RMS of 176 and an average value of 387 counts. (The manufacturer recommends a minimum of 25 and 80 for RMS and intensity counts respectively.) The images were correlated using the LaVision DaVis DIC software. Initially cell sizes of 64 x 64 pixels were used, as was identified in [7] as providing sufficient strain accuracy with the LaVision software. It should be noted that the resolution of the Motion pro camera is significantly less than those used in [7] for image correlation with low speed data capture. The use of a different camera system prompted a further investigation into the effect of cell size. The LaVision correlation algorithm only allows data to be processed using cell sizes of powers of two; all cell sizes from 4 x 4 to 64 x 64 were examined. All but the 32 x 32 and 64 x 64 contained large amounts of noise. The results for 32 x 32 and 64 x 64 for a 0° and 90° surface ply are shown in Figures 5 and 6 respectively. The data represent the moment before failure as the image before complete specimen failure is used for the correlation. The 90° surface ply specimen failed at a load of 11.3 kN and the 0° surface ply specimen failed at a load of 10.1 kN. It would be extremely difficult to capture this data without a high speed camera. For the 64 x 64 cell size which represented 1.52 mm^2 on the specimen, the strain is uniform but there is no definition around the notch. The 32 x 32 represent a smaller area of 0.76 mm^2 . The data has better spatial resolution but more noise. A compromise was found by using 64 x 64 cell size with 75% overlap in the cells; this smoothed the data but enabled much more definition at the notch. The results are shown in Figure 7 for 0° and 90° surface plies respectively.

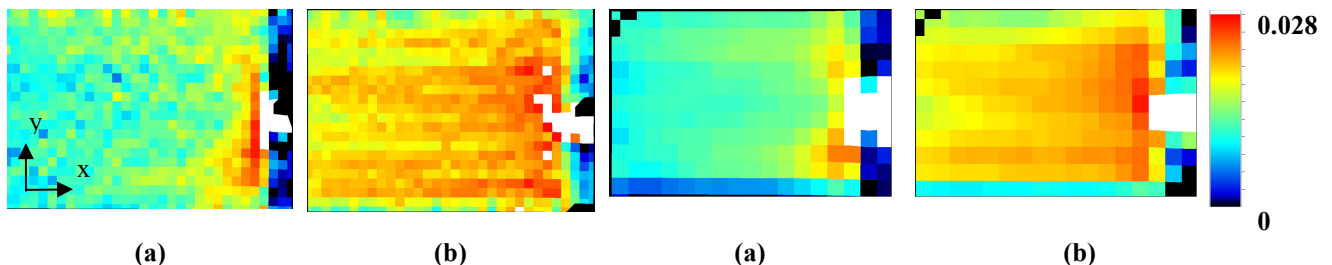


Figure 5: Strain map (ϵ_{yy}) using a 32 x 32 cell size for a 0° surface ply specimen (a) (Image area = 457 mm²), and a 90° surface ply specimen (b) (Image area = 462 mm²)

Figure 6: Strain map (ϵ_{yy}) using a 64 x 64 cell size for a 0° surface ply specimen (a) (Image area = 457 mm²), and a 90° surface ply specimen (b) (Image area = 462 mm²)

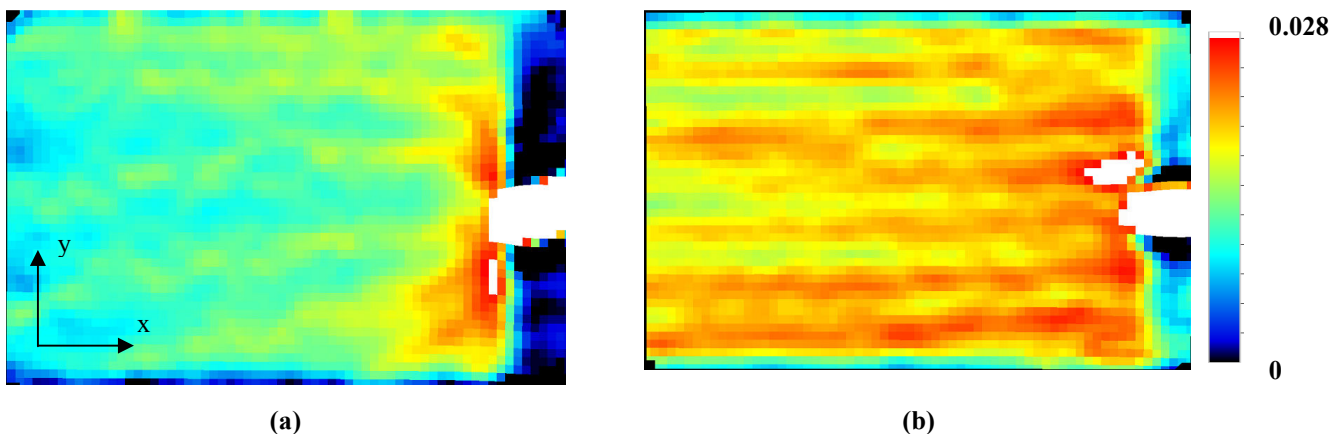


Figure 7: Strain map (ϵ_{yy}) using a 64 x 64 cell size with 75% overlap for a 0° surface ply specimen (a) (Image area = 457 mm²) and a 90° surface ply specimen (b) (Image area = 462 mm²)

Figure 7 shows data related to the longitudinal strain. The TSA data is related to a combination of the principal stresses and coefficients of thermal expansion (see Equation (1)). Therefore a direct comparison of the two is not possible. However it is clear that in Figure 7a there are strain concentrations occurring at the crack and in Figure 7b the data is showing overall ply failure. The resolution of the TSA data is far superior but it does not deliver component direct strains. However, a combination of the two techniques could be used to evaluate the material condition and provide better insight into the material failure.

Conclusions and future work

Some of the limitations and advantages of DIC and TSA have been demonstrated in this paper with several useful properties being confirmed for cross-ply laminates. The decreasing load carrying capacity of a 90° surface layer has been shown through the formation of transverse cracks and inversely the increased stress and consequently a more dramatic stress concentration effect at the notch with a 0° surface layer. Spatial resolution and internal camera storage capacity have been found to be a key limitation for the high speed camera system used. However, it has been clearly demonstrated that the high speed DIC can capture the strain state just prior to material failure. A direct comparison of strain derived from the DIC using high resolution cameras at each load step used in the TSA is the next step in the process. By following the same load steps as in the TSA experiments and calibrating the thermoelastic response with this material, the stress patterns could be compared directly.

Acknowledgements

The work described in this paper is supported by the UK Engineering and Physical Sciences Research Council (Grant number EP/G042403/1) and DSTL under a joint grant managed programme on damage tolerance.

References

- [1] T. L. Anderson: *Fracture Mechanics Fundamentals and Applications*, (Taylor and Francis Group Publishing, 2005).
- [2] J. F. Caron and A. Ehrlacher, *Composites Science and Technology* Vol. 57 (1997), p. 1261-1270.
- [3] J. Dulieu-Barton and P. Stanley, *Journal of Strain Analysis for Engineering Design* Vol. 33 (1998), p. 93-104.
- [4] R. K. Fruehmann, J. M. Dulieu-Barton and S. Quinn, *Journal of Strain Analysis for Engineering Design* Vol. 43 (2008), p. 435-450.
- [5] M. Grédiac, *Composites Part A: Applied Science and Manufacturing* Vol. 35 (2004), p. 751-761.
- [6] M. Zanganeh, R. A. Tomlinson and J. R. Yates, *Journal of Strain Analysis for Engineering Design* Vol. 43 (2008), p. 529-537.
- [7] D. Khennouf, J. Dulieu-Barton, A. R. Chambers, F. J. Lennard and D. D. Eastop, *Strain* Vol. 46 (2010), p. 19-32.