# Tool Wear Intelligence Measure in Cutting Process Based on HMM

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**Abstract**- A method of tool wear intelligence measure based on Discrete Hidden Markov Models (DHMM) is proposed to monitor tool wear and to predict tool failure. FFT features are first extracted from the proposed and cutting force in cutting process, and then FFT vectors are presorted and convert d into intensity by SOM. Finally, these codes are introduced to DHMM for machine learning and 3 models for efferent tool year stage are built up. Pattern of HMM is recognised by calculating probability. The result of tool wear intelligence measure and pattern recognition of tool wear experiments show that the method is extinct.

## Introduction

If tool wear take place in the cutting process, the information of ool car will be down in the signal of cutting process. We monitor tool wear and predict the tool ciliure to be cutting process, so that reasonable measures can be taken to eliminate failure in early period. Thus, conitoring of tool wear is always paid great attention to, and there have been researches on features extracted from the vibration signal to monitor tool wear, failure prediction and recognition based on dynamic signal of cutting force, and tool wear monitor using AE sensor, etc[1,2,3], whese methods are based on recognition of narrow-band features from the spectrum, wavelet analysis, and network and dynamic tree. The availability of these methods highly relies on the regions of feature selection and the rationality of judging threshold [3,4,5]. The effect and conclusion of too wear monitoring based on DHMM were reported by reference [1] and [2]. Reference [6] and [7] present the fault diagnosis method based on

## Tool Wear Intelligence Measure Tool Wear Intelligence Measure

If we get the survival probability of tools car known as prior probability, we could judge the tool wear pattern by selecting maxicum survival probability  $\max\{P(\omega)\}$ . However, the judgment is not reasonable. Felicitous way is to judy by using conditional probability  $P(\omega|\Phi t-k)$  known as posterior probability, because it is calculated on prior probability  $P(\omega)$  and observation sequence of tool wear process  $\Phi t-k$ . Path recognition of tool wear is to find a model  $\hat{\omega}$  and to calculate  $\max\{P(\omega|\Phi t-k)\}$  in judging recess. But d or Bayesian, posterior probability is calculated by (1)

$$P(\omega_{|\cdot|}) = P(\Phi_{t-k}|\omega)P(\omega)$$

$$P(\Phi_{t-k})$$
(1)

Practically, to prior probability  $P(\omega)$  is difficult. So we take the process as average probability event and have the following relation:

$$\sum_{j=1}^{c} P(\omega) = 1 \tag{2}$$

Posterior probability  $P(\omega|\Phi t-k)$  is known as maximum likelihood estimation of  $\omega$  adapted to sample gather. That is to say, model  $\omega$  can get the max $\{P(\omega|\Phi t-k)\}$  in corresponding observation sequence[3,5].A HMM is a kind of statistic modeling tool for time sequence, whose application in speech recognition, faults diagnosis and computational biology processing is successful. HMM accomplishes statistic of non-stationary signal and parameterized modeling, and it can be used easily

in probability reasoning. Therefore, HMM is a useful tool for dynamic pattern classification. In the cutting process, when tool wear take place, the vibration features change with the stages. The changes of vibration signal are represented statistically by HMM so that the whole vibration pattern of wear process will be clear.

HMM comprises two parts: Markov chain and stochastic process. Markov chain, whose output is a sequence of state, can be described by  $\pi$  and A, while stochastic process whose output is a sequence of observed values, is described by B. Thus, a HMM can be described as:

$$\lambda = (N, M, \pi, A, \mathbf{B}) \tag{3}$$

A HMM is described by parameters defined below:

- 1) N: state number of Markov chain.  $\theta_1, \theta_2, \cdots, \theta_N$  are the possible states of Markov chain and  $q_i$  is the teat time t, so we get  $q_i \in (\theta_1, \theta_2, \cdots, \theta_N)$ .
- 2) M: possible number of observed value in each state. If  $v_1, v_2, \dots, v_M$  are the observed values value at time t, then  $o_t \in (v_1, v_2, \dots, v_M)$ .
- 3)  $\pi$ : initial probability distribution vector,

where 
$$\pi_i = P(q_t = \theta_i), 1 \le i \le N$$

4) A: state shift probability matrix, 
$$A = (a_{ij})_{N \times N}$$
 (4) where  $a_{ij} = P(q_{t+1} = \theta_i / q_t = \theta_i)$   $1 \le i, j \le N$ 

5) B: probability matrix of observed values, 
$$\mathbf{B} = (b_i)_{N \times M}$$
 (5) where  $b_{ik} = P(o_t = v_k / q_t = \theta_i), 1 \le j \le N, 1 \le k \le M$ 

The estimation formulas of Viterbi algorithm are based on the frequency under which different observed event occurs. Therefore, estimation formulas of multiple observed samples can be obtained by adding every frequency under which in event occurs independently. The adapted Baum-Welch re-estimation formulas with k simple treatment of the obtained, which are reasoned out in reference [6]. More details on HMM on be found in [6, 7, 8].

To make the model more rob, we need paltiple samples to train the model so that the re-estimation formulas have to be adapted. Suppose the sequence of K observed samples is

$$\mathbf{O} = [\mathbf{O}^{(1)}, \mathbf{O}^{(K)}, \cdots, \mathbf{O}^{(K)}] \tag{6}$$

where  $\mathbf{O}^{(k)} = [\mathbf{o}_1^{(k)}, \mathbf{o}_2, \cdots, \mathbf{o}_t^{(k)}, \mathbf{o}_{T_k}^{(k)}]$  is the K st sample whose sample length is Tk, we know that every sample is an edered see of a vector series. In modeling of vibration signal we use samples of equal length,  $\mathbf{b} = \mathbf{T}$ . Suppose that each sample is independent, the goal of model training is to adapt the parameter. To yield a maximum of the value below

$$P(\boldsymbol{O} \mid \lambda) = \prod_{k=1}^{K} P(\boldsymbol{O}^{(k)} \mid \lambda) = \prod_{k=1}^{K} P_{k}$$
(7)

## DHMM of Tool Wear & Recognition Method

To recognize different states of tool wear, DHMM models for all possible wear state except tool sharp state, should be trained. Thus, a model library is formed. To recognize wear states, pretreatment of vibration signal and dynamic portion of cutting force (FFT, feature extraction and vector coding) is needed. Then we calculate the probability of each output of models in the library, and choose the maximum, in this way wear state is recognized.

Because the spectrum vectors of different states are obviously different, tool wear process from sharp, workable to dull can be simulated by a 8-state DHMM according to the DHMM theory, as illustrated in fig.1. The figure illustrates 8 states and the relation between states and variables, where aij, i, j=1,2,...8 is the state transfer probability, ot is the observed code at time t, or the serial number of excitatory neuron which is the output of FFT spectrum vector after mapping. Method of feature extraction in fig.2 can be selected in light of requirement. c is the total number of tool wear process types, and it can be increased when necessary. FFT-DHMM recognition of tool wear can be described as below:

(1)Acquisition of spectrum sequence To be used in training, several wear processes are needed. In the k st process, T frames of signal are acquired. Spectrum feature is extracted from every frame, and the spectrum vector sequence of the whole process can be written as

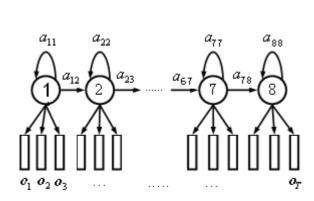
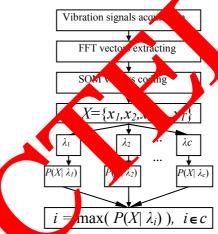


Fig. 1 DHMM Structure of tool wea



1g.2 Flowchart of wear state

$$X^{(k)} = [x_1^{(k)}, x_2^{(k)}, \cdots x_t^{(k)}, x_T^{(k)}]$$
(8)

where  $x_t^{(k)}$  is the t st spectrum frame of the k st process.

(2) Quantification of observe sequence wery spectrum is normalized and coded so that a discrete set of codes is formed. Suppose set the quantified sequence of spectrum is ot, where  $1 \le t \le T$ . Thus, the coded vector of the t stespectrum tame of the k st process is  $\boldsymbol{o}_t^{(k)}$ . The observed sequence set after quantifying the lattice and plot of the k st process is

$$\mathbf{O}^{(k)} = [\mathbf{o}^{(k)}, \mathbf{o}^{(k)}_{2}, \cdots, \mathbf{o}^{(k)}_{p}, \mathbf{o}^{(k)}_{p}]$$
(9)

- (3) Dr. Mt sining Considering the underflow of algorithm, iterative algorithm is used to calculate the DHM parameters by adapted multiple sequence re-estimation formulas [8]. After feature extraction and SOM vector coding, DHMM for tool sharp state, workable and dull can be modeled.
- (4)Recognition of tool wear After modeling DHMM of different wear state, Viterbi algorithm [8] can be used to calculate and recognize tool wear states. The current observed sequence is submitted into DHMM of different state. Then we calculate the reasoning probability  $P(O \mid \lambda)$  with which current sequence turns up in the state by Viterbi algorithm. Finally, we know the current state whose probability  $P(O \mid \lambda)$  is the largest. In this way, wear state can be recognized.

## **Experiment of Tool Wear Distinguishing**

To confirm the availability of tool wear intelligence measure in failure prediction and wear monitoring, we did cutting test on lathe (CA6140) during which DHMMs for initial wear stage, normal wear stage and severe wear stage were modeled.

#### Test condition and detection device

In the test, the dynamometer (YDC-III) is used to detect main cutting force Fz(t), accelerometer (B&K4370) on the toolbar is used to detect tool vibration a(t). Charge amplifier and filter are used as pretreatment of signal. Cutting force signal Fz(t) and cutting tool vibration signal a(t) are sampled by IPC with A/D convertor.

The cutting conditions are:  $v=1.5\sim2m/s$ , f=0.41mm/r, ap=1mm. The cutting tool parameters are  $\gamma o=12^{\circ}$ ,  $\kappa=45^{\circ}$ ,  $\alpha n=8^{\circ}$ ,  $\lambda s=0$ . the material of cutting tool is YT15. Testing material is 45# steel and its hardness is HB243.

# Feature vector selection and SOM coding

In the experiment, we sampled the signals of cutting force Fz(t) and vibration of cooled different conditions of wear amount of tool, and then transformed the signals by me as of FFT. the feature signal is abstracted, and the power spectrum of signals in different wear re is shown in fig.3 and fig.4 The figure shows that high frequency component of the vibration acc direction increases obviously with the increase of tool wear amount while component changed little; the amplitude of dynamic component of cutting rce signal Fz(t) and the high frequency component increase with the increase of the wear amount intensity gets higher. By analyzing the feature of signals and calcaling the rele Besides, the power the signal feature and the wear amount, we determine to take the power pectrum vectors of dynamic component of cutting force signal and the vibration acceleration on signal cutter bar as the feature vectors.

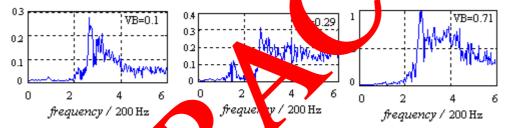


Fig. 3 normalized wer sectrum of signal Fz(t) in different wear stage

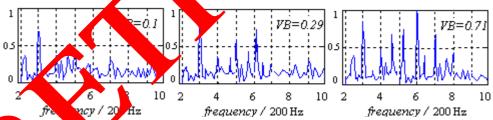


Fig. no malized power spectrum of signal a(t) in different wear stage

To complete the form of different wear stages, we normalized the spectrum amplitude of different wear stages efore the scalar qualification. Then the amplitude is limited within the range of  $0 \sim 1$ . That is:

$$x(i) = \{x(i) - \min[x(i)]\} / \{\max[x(i)] - \min[x(i)]\}$$
(10)

When coding the SOM vectors, the feature vectors were qualified and coded to make an observed sequence O. Thus, we realized the compression of redundant information. When code is 40-graded, the coding result of normalized spectrum vectors is shown in tab.1.

## Model training and wear stage recognition

In the training of DHMM, we used 10 samples from each group, to have a robust model. The group is respectively VB=0.1mm, VB=0.4mm and VB=0.7mm, representing three wear stages. We used Baum-Welch algorithm of multi-observation revaluation to revaluate the modification formulation

and train the DHMM. Usually, training for 30-50 times can reach the precision acquired. We obtained DHMM of different wear stages, written as  $\lambda 1$ ,  $\lambda 2$ ,  $\lambda 3$  respectively. Then the three groups of primary parameters  $\pi i$ , aij and bij can be taken as the parameters of DHMM to monitor the wear stage of tool.  $\pi i$  is the probability distribution parameter of initial state, that is

$$\pi = [1, 1.8802e - 85, 2.2043e - 95, 6.2566e - 64, 0]$$

It shows that initial state of the given observed sequence for training is 1, and the probability of other states to occur is almost zero. For the convenience of calculating, we suppose

 $\pi$ =(1,0,0,0,0). The training result of aij, bij is neglected due to the length of paper, and the process is explained in reference [6]. Submit the observed sequence into equation.(11), we obtain the probability of the sequence, P(Ot |  $\lambda$ i) i=1,2,3. To recognize the wear stages of tool, we have

$$\max_{t=1,2,\dots,T} [P(\boldsymbol{O}_t \mid \lambda_i)]$$
 (i=1,2,3),

The typical output of logarithmic probability and the recognition result are shown in tab.

Take typical recognition as example, when VB=0.29 we obtained logP( $C_1 \lambda I_2$ )= -3439, logP(Ot |  $\lambda I_2$ )= -19.38 and logP(Ot |  $\lambda I_3$ )= -75.06 at the observed sequence Ot, and maxL(Ot |  $\lambda I_3$ )] is obtained when i=2. Therefore, normal wear stage was recognised then tool is a gnised in severe wear stage, that is to say, P(Ot |  $\lambda I_3$ ) reaches the maximum, he can ge force and vibration will increase severely, and the tool failure will take place in soor.

Table 1 Coding result of normalized spectrum

Table typical out of wear process in log(P)

Feature sample Frequency Hz		603	807	1041	1212	1407	Output		$\lambda_2$	λ <sub>3</sub>	Recognition result
Initial	Amp.	0.71	0.37	0.45	0.21	0.35	0.10	- <b>16.59</b>	-21.68	-97.23	initial wear
wear	Coding	29	15	18	9	14	94	-21.46	-18.32	-84.59	normal wear
Normal wear	Amp.	0.77	0.41	0.55	0.74	024	0.3 0.29 0.4 0.4		-19.38 -15.89	-75.06 -59.98	normal wear normal wear
	Coding	31	17	23	29	10	0.50	0 -51.78	-27.53	-45.57	normal wear
Severe wear	Amp.	0.79	0.52	0.77	1		0.6 0.62 0.7 0.7		<b>-32.62</b> -69.62	-38.73 <b>-11.38</b>	normal wear severe wear
	Coding	32	21	31		29	0.8 0.79	9 -98.47	-85.23	-15.27	severe wear

### Conclusion

- A. The signal of tool wear process from initial wear stage, normal wear stage to severe wear stage is non-stationary. The non-stationary process can be described by statistic model DHMM and its states can be sorted in method of probability. Tab.1~2 show it effective to recognize different wear states in method of the probability of probability.
- B. Tracing a DHMM is simple. Because SOM preserves the topology in vector projection, we transform cobserved FFT spectrum vector into SOM quantified code.
- C. When cuting conditions, such as cutting parameters, cutting tool material and parameters, workpiece material change, new DHMM training is necessary. For different tool wear criteria, corresponding VB are need to be adapted.
- D. For trained DHMM, the interval from sampling to recognising is about 100~200ms. Therefore, the tool wear monitoring and tool failure prediction based on hybrid SOM-DHMM architecture can be used to monitor tool wear online.

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