

The Effect of Radiation on Free Convection from a Heated Horizontal Circular Cylinder

Najahulfazliah Zainuddin¹, Ishak Hashim², Muhaimin Ismoen¹
& Rozaini Roslan¹

¹ Centre for Research in Computational Mathematics
Faculty of Science, Technology and Human Development
Universiti Tun Hussein Onn
86400 Batu Pahat, Johor DT, Malaysia

²Centre for Modelling & Data Analysis, School of Mathematical Sciences
Universiti Kebangsaan Malaysia
43600 UKM Bangi, Selangor DE, Malaysia

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Abstract. Effect of radiation on free convection on heated horizontal circular has been investigated. The cylinder is fixed and immersed in a stationary fluid, in which the temperature is uniformly heated about the temperature of the surrounding fluid. The governing equation are transformed into dimensionless non-linear of partial differential equations and solved numerically by employing a finite difference method. An implicit finite difference scheme of Crank Nicolson method is used to analyze the results. This study determine the effects of radiation parameter, R_d heat generation parameter, γ and the Prandtl number, Pr , on the temperature and velocity profiles. The results of the local heat transfer and skin-friction coefficient in the presence of radiation for some selected values of Prandtl number and heat generation parameter have shown graphically.

INTRODUCTION

The effects of radiation on free convection boundary layer over a various shapes such as plate, sphere, cylinder and others have been studied among researchers because it has become more important in recent years. The reason is the thermal radiation effects on free convection flow are important in engineering applications, such as in advanced types of power plants for nuclear rockets, high-speed flights, re-entry vehicles and processes involving high temperature. The effect of heat generation in convection is also important and significant where there exist difference temperature between the surface and the ambient fluid. In certain applications on dealing with heat generation may alters the temperature and velocity distribution.

As the presence of heat generation where there is the difference between the surface temperature and the ambient temperature, the radiation effects is also important. In the study on the effect of radiation on free convection was studied by Soundalgekar et al. (1960) which consider on free convection flow of a gas past a semi-infinite flat plate using the Cogley et al. (1968) equilibrium model. While, Hossain & Takhar (1996) have analyzed the effects of radiation on free convection flow past a heated vertical plate. Later Tahmina & Alim et al. (2008) extended from the previous studies on a sphere with uniform surface heat. Besides that, Yih (1999) studied on a truncated cone by following the Rosseland diffusion approximation which also used by Molla et al. (2009b) on investigate the radiation effect on natural convection over vertical wavy frustum of cone. Then, Molla et al. (2011) extended their previous study on a horizontal circular cylinder. The radiative heat fluxes can be approximated by the Rosseland diffusion approximation which has been employed among researchers. Very recently, Elbashbeshy et al. (2014) was considered on the effect of heat generation or absorption and thermal radiation on free convection flow and heat transfer over a truncated cone in the presence of pressure work.

Furthermore, the study on free convection with the presence both of heat generation and radiation on natural convection flow over a various type of shape was investigated. The study on a sphere was investigated by Miraj & Alim (2010). Later, Miraj et al. (2011) extended his previous work to investigate the effects of pressure work and radiation on their problem. While, Makinde (2012) study on the hydromagnetic mixed convection stagnation point flow towards a vertical plate embedded in a highly porous medium. Recently, Ali et al. (2013) investigate MHD free convection flow along vertical flat plate. While, Ferdousi et al. (2013) studied on a porous vertical plate in presence of heat generation.

Ganesan & Rani (1998) presented a numerical solution for the transient natural convection flow over a vertical cylinder under the combined buoyancy effects of heat and mass transfer by employing an implicit finite-difference method that has been used by Rani & Devaraj (2003) in studied about unsteady flow past a vertical cylinder with temperature oscillations. A finite difference method is also presented in Abd El-Nabyet al. (2004) work who studied on radiation effects on MHD unsteady free convection flow over vertical porous plate. Rani & Kim (2008) are also demonstrate the Crank-Nicolson type of implicit finite- difference method in their study on the transient free convection flow over an isothermal vertical cylinder with temperature dependent viscosity. The above method is also used by Reddy & Reddy (2009a) and Reddy & Reddy (2009b) on the interaction of radiation and mass transfer effects on unsteady MHD free convection flow past a semi-infinite moving vertical cylinder. Recently, Ismail et al. (2012) demonstrated a finite difference solution of radiation on unsteady free convective magnetohydrodynamic flow past a vertical cylinder with heat and mass transfer. They solve their problem by an implicit finite difference scheme of Crank-Nicolson method which is demonstrated in Velusamy & Garg (1992) work. Very recently, Udin & Harmand (2013) employed the an unconditionally stable implicit finite difference scheme to solve their problems on unsteady natural convection heat transfer of nanofluid along a vertical plate embedded in porous medium.

There was another works that solved numerically by using explicit finite difference method that demonstrated in Carnahan et al. (1969) in studied about free convection on a heated plate. The method has been used by Udin & Kumar (2010) in the problem of unsteady free convection in a fluid past an inclined plate immersed in a porous medium. Besides that, the method is also has been employed by Khan et al. (2012) in his studied on unsteady MHD free convection boundary- layer flow of a nanofluid along a stretching sheet with thermal radiation and viscous dissipation effects.

In the present study, it is considered to investigate the natural convection flow on a heated horizontal circular cylinder in the presence of heat generation and radiation by employing the Rosseland diffusion approximation. The governing equations of this study are transformed into dimensionless forms, which are solved numerically using a Crank-Nicolson type implicit finite-difference. The numerical results have been obtained in terms of local skin friction, rate of heat transfer, velocity profiles as well as temperature profiles for set of different radiation parameter, heat generation parameter and Prandtl number.

FORMULATION OF PROBLEM

Free convection flow from a heated horizontal circular cylinder in the presence of radiation is considered. The flow over the horizontal circular cylinder is assumed to be two-dimensional, laminar, unsteady and incompressible. The physical configuration is as shown in the Figure 1.

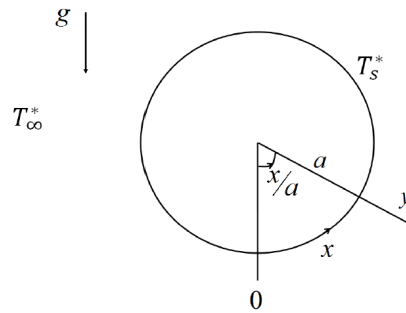


Figure 1: Physical model of circular cylinder

T_s^* is assumed as the surface temperature of the cylinder where $T_s^* > T_\infty^*$ and T_∞^* is assumed as the ambient temperature of the fluid and T^* is the temperature of the fluid. By extending the problem of free convection on heated plate by Carnahan et al. (1969) and the problem of the effect of on free convection over the circular cylinder from Molla et al. (2011) and Miraj & Alim (2010), respectively are considered. By considering the present physical conditions, usual Boussinesq approximation and boundary layer approximations, the full of continuity, momentum and energy equations are formulated in the following forms:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0, \quad (1)$$

$$\frac{\partial u}{\partial t^*} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = \nu \left(\frac{\partial^2 u}{\partial y^2} \right) + g\beta(T^* - T_\infty^*) \sin\left(\frac{x}{a}\right), \quad (2)$$

$$\frac{\partial T^*}{\partial t^*} + u \frac{\partial T^*}{\partial x} + v \frac{\partial T^*}{\partial y} = \frac{\kappa}{\rho C_p} \left(\frac{\partial^2 T^*}{\partial y^2} \right) - \frac{1}{\rho C_p} \left(\frac{\partial q_r''}{\partial y} \right), \quad (3)$$

where the x -coordinate is defined as a distance measured along the surface of a circular cylinder in vertically upward direction and y -coordinate is the outwards a distance measured normally from the surface of the cylinder. u and v denote the velocity components in the x and y directions, respectively. The gravitational acceleration g is acting downward and β is the coefficient of thermal expansion, (x/a) is the angle of the y -axis, T^* is the temperature of fluid and T_∞^* is the temperature away from the cylinder, κ is the thermal conductivity, ρ is the fluid density, C_p is the specific heat of constant pressure, and q_r'' represents the radiative heat flux in the y direction. The boundary conditions are taken as

$$\begin{aligned} v &= 0, \quad T^* = T_s^* \quad \text{at} \quad y = 0, \\ u &\rightarrow 0, \quad v \rightarrow 0, \quad T^* \rightarrow T_\infty^* \quad \text{as} \quad y \rightarrow \infty. \end{aligned} \quad (4)$$

In equation (3), the term q_r'' the radiative heat flux which is as Rosseland diffusion approximation obtained by Rosseland (1936) and is given by

$$q_r'' = \frac{4\sigma}{3\kappa(\alpha_r + \sigma_s)} \frac{\partial T^{*4}}{\partial y}, \quad (5)$$

Where σ the Stefan-Boltzmann constant, α_r is Rosseland mean absorption coefficient and σ_s is the scattering coefficient. The above expression that measures the radiative heat transfer, q_r'' is appropriate

for two-dimensional boundary layer flow. In order to non-dimensionalize equations (1)–(4) the following dimensionless variables are introduced:

$$\begin{aligned} X &= \frac{x}{a}, \quad Y = \frac{y}{a} Gr^{1/4}, \quad t^* = \frac{a^2}{\nu} Gr^{-1/2} t, \quad U = \frac{a}{\nu} Gr^{1/2}, \quad V = \frac{a}{\nu} Gr^{-1/4} v, \\ T &= \frac{T^* - T_\infty^*}{T_s^* - T_\infty^*}, \quad Gr = g\beta \frac{(T_s^* - T_\infty^*)}{\nu^2} a^3, \\ T_s &= \frac{T_s^*}{T_\infty^*}, \quad \Delta = T_s - 1, \quad R_d = \frac{4\sigma T_\infty^{*3}}{\kappa(\alpha_r + \sigma_s)}, \quad = \frac{\mu}{\rho}, \quad = \frac{\mu C_\rho}{k}, \end{aligned} \quad (6)$$

where ν is the reference kinematic viscosity, Gr is the Grashof number, T is non-dimensional temperature function, T_s is the surface temperature parameter, R_d is radiation parameter, Pr is the Prandtl number. Convert the governing equations (1)-(3) and the boundary conditions (4) into dimensional forms by substituting the non-dimensional variables above into the equations (1) – (4) and becomes to the following form:

$$\frac{\partial U}{\partial X} + \frac{\partial V}{\partial Y} = 0, \quad (7)$$

$$\frac{\partial U}{\partial t} + U \frac{\partial U}{\partial X} + V \frac{\partial U}{\partial Y} = \frac{\partial^2 U}{\partial Y^2} + \sin X, \quad (8)$$

$$\frac{\partial T}{\partial t} + U \frac{\partial T}{\partial X} + V \frac{\partial T}{\partial Y} = \frac{1}{Pr} \frac{\partial}{\partial Y^2} \left[\left\{ 1 + \frac{4}{3} R_d (1 + \Delta T)^3 \right\} \frac{\partial T}{\partial Y} \right]. \quad (9)$$

The corresponding boundary conditions in dimensionless form are as follows:

$$\begin{aligned} U &= V = 0, \quad = 1 \quad \text{at } Y = 0, \\ U &\rightarrow 0, \quad V \rightarrow 0, \quad \rightarrow 0 \quad \text{as } Y \rightarrow \infty. \end{aligned} \quad (10)$$

The physical quantities of principle interest are the rate of heat transfer and the shearing stress, τ_s in terms of the Nusselt number, Nu and skin-friction coefficient, C_f respectively, which can be written as

$$Nu = \frac{a(q_s'' + q_r'')_{y=0}}{\kappa(T_s^* - T_\infty^*)}, \quad C_f = \frac{(\tau_s)_{y=0}}{\rho U_\infty^2}, \quad (11)$$

where $\tau_s = \mu(\partial u / \partial y)$ and $q_s'' = -k(\partial T^* / \partial y)$. By using the non-dimensional variables (6) into equations (11) made the equation becomes in dimensionless forms:

$$Nu Gr^{-1/4} = - \left(1 + \frac{4}{3} R_d T_s^3 \right) \frac{\partial T}{\partial Y} \Big|_{Y=0}, \quad (12)$$

$$C_f Gr^{1/4} = X \frac{\partial^2 T}{\partial Y^2} \Big|_{Y=0}. \quad (13)$$

An implicit finite difference scheme of Crank Nicolson type is employed to solve the non-linear partial differential equations (7)-(9) under the boundary conditions (10). The region of solution is considered from the beginning of stagnation point $X = 0$ to the end stagnation point $X_{max} = \pi$ and an

axis normal to the surface from $Y = 0$ to $Y_{max} = 30.0$ as corresponding to Y_{∞} . The subscripts i and j designate the grid points along the X and Y coordinates, respectively where $X_i = i\Delta X$ and $Y_j = j\Delta Y$ and the subscript k designates the value of time $t = k\Delta t$ with the mesh sizes $\Delta X = \pi/150$, $\Delta Y = 0.12$ with the time step size dependency of $\Delta t = 0.01$. The iterative procedure is stopped when the time step reached to $t_{max} = 10$. The finite difference equations corresponding to equations (7)-(9) are as follows:

Crank-Nicolson method

The equations (7)-(9) subject to the boundary conditions (10) are discretized using Crank-Nicolson types of implicit finite difference method and finally the system of tri-diagonal system of equations are obtained. Such a system of equations solved by Thomas algorithm as described in Carnahan et al. (1969).

$$\frac{1}{2} \left[\frac{V_{i,j}^{k+1} - V_{i,j-1}^{k+1}}{\Delta Y} + \frac{V_{i,j}^k - V_{i,j-1}^k}{\Delta Y} \right] = \frac{1}{2} \left[\frac{U_{i,j}^{k+1} - U_{i-1,j}^{k+1}}{\Delta X} + \frac{U_{i,j}^k - U_{i-1,j}^k}{\Delta X} \right], \quad (13)$$

$$\begin{aligned} \frac{U_{i,j}^{k+1} - U_{i,j}^k}{\Delta t} + \frac{1}{2} \left[U_{i,j}^k \left(\frac{U_{i,j}^{k+1} - U_{i-1,j}^{k+1} + U_{i,j}^k - U_{i-1,j}^k}{\Delta X} \right) + V_{i,j}^k \left(\frac{U_{i,j}^{k+1} - U_{i,j-1}^{k+1} + U_{i,j}^k - U_{i,j-1}^k}{\Delta Y} \right) \right] \\ = \frac{1}{2} \left[\left(\frac{U_{i,j+1}^{k+1} - 2U_{i,j}^{k+1} + U_{i,j-1}^{k+1} + U_{i,j+1}^k - 2U_{i,j}^k + U_{i,j-1}^k}{\Delta Y^2} \right) \right. \\ \left. - (T_{i,j}^{k+1} + T_{i,j}^k) \sin X_i \right], \quad (14) \end{aligned}$$

$$\begin{aligned} \frac{T_{i,j}^{k+1} - T_{i,j}^k}{\Delta t} = \frac{1}{2} \left[-U_{i,j}^k \frac{T_{i+1,j}^{k+1} - T_{i-1,j}^{k+1} + T_{i+1,j}^k - T_{i-1,j}^k}{2\Delta X} - V_{i,j}^k \frac{T_{i,j+1}^{k+1} - T_{i,j-1}^{k+1} + T_{i,j+1}^k - T_{i,j-1}^k}{\Delta Y} \right] \\ + \frac{1}{2} \left[\frac{1}{Pr} \frac{\partial}{\partial Y} \left[\left\{ 1 + \frac{4}{3} R_d (1 + (T_s - 1) T_{i,j}^k)^3 \right\} \left(\frac{T_{i,j}^{k+1} - T_{i,j-1}^{k+1} + T_{i,j}^k - T_{i,j-1}^k}{\Delta Y} \right) \right] \right]. \quad (15) \end{aligned}$$

NUMERICAL RESULTS

The numerical results of study on free convection on a heated horizontal circular cylinder in the presence of heat generation are presented. This work was considered the effect of radiation parameter and heat generation parameter on the rate of heat transfer, the skin-friction coefficient, the temperature and velocity profiles. The effect of different Prandtl number will also be presented. Here, the Prandtl number used are $Pr = 0.7, 4.0, 7.0$ and the effects of radiation parameter $R_d = 0.0, 0.2, 0.5, 1.0$. The numerical results of the local heat transfer or Nusselt number and the local skin-friction coefficient are obtained in Table 1 represented the comparisons between of the present study with the previous study Molla *et al.* (2011). Here, Prandtl numbers $Pr = 0.73$, has been chosen. It is observed from the table that the present result has a good agreement with the results of Molla *et al.* (2011).

The effect for different values of radiation parameter R_d on the velocity and temperature profiles with $Pr = 0.7$ and surface temperature parameter $T_s = 1.0$ are shown in Figures 1 and 2. Here, as R_d increase, both the velocity and the temperature increase because the thermal boundary layer thickness increases and the thickness of the velocity boundary layer also increase. Which means the velocity and temperature gradients at the surface increase enhances the fluid velocity and temperature. The local maximum of the velocity exist within the boundary layer, but velocity increases

near the surface of the cylinder and then decrease slowly approaches to zero while, the temperature from the surface decreases slowly and finally tend to zero. The change of velocity and temperature profiles in the Y direction satisfied the natural convection boundary layer flow.

TABLE 1. Comparison between the present results and the previous study by Molla et al. (2011) for the rate of heat transfer $NuGr^{-1/4}$ and the local skin friction coefficients $C_fGr^{1/4}$ when $T_s = 1.1$, $R_d = 0.5$ and $Pr = 0.73$.

X	$NuGr^{-1/4}$		$C_fGr^{1/4}$	
	Present study	Molla et al. (2011)	Present study	Molla et al. (2011)
0	0.54492	0.54424	0.0000	0.0000
$\pi/6$	0.53773	0.53776	0.46937	0.46890
$\pi/3$	0.51852	0.51845	0.86103	0.85457
$\pi/2$	0.48592	0.48592	1.07755	1.08646
$2\pi/3$	0.43871	0.43887	1.11688	1.11449
$5\pi/6$	0.37512	0.37391	0.92132	0.91093
π	0.27337	0.27466	0.44234	0.44387

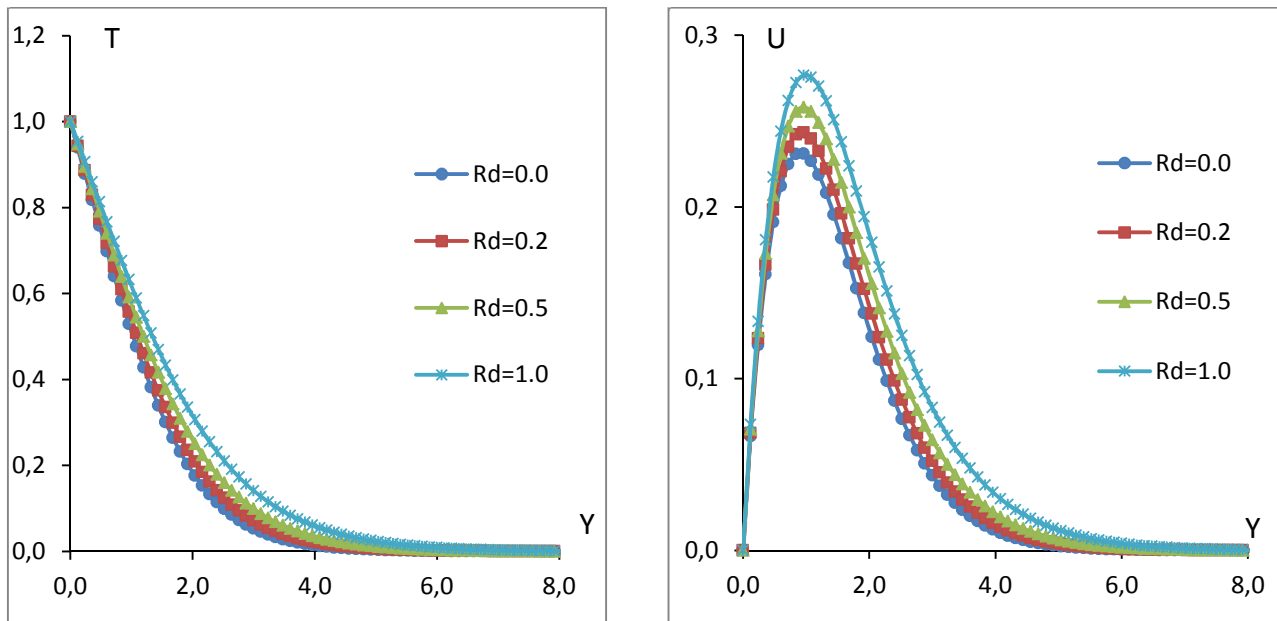


FIGURE 1. Temperature profile against Y with $\gamma = 0.0$ and $Pr = 0.7$ at $t = 4.0$ and $X = \pi/6$. FIGURE 2. Velocity profile against Y with $\gamma = 0.0$ and $Pr = 0.7$ at $t = 4.0$ and $X = \pi/6$.

Figures 3 and 4 show the local rate of heat transfer Nu and the local skin-friction coefficient C_f respectively, increase for increasing values of R_d , while $Pr = 0.7$ and $t = 4.0$. It is found that from the Figure 4, the skin friction increase gradually from zero value at beginning stagnation point $X = 0$ along the X direction and slowly decrease to downstream point $X_{max} = \pi$. From Figure 3, it reveals that the rate of heat transfer decrease slightly along the X direction from beginning stagnation point to the downstream.

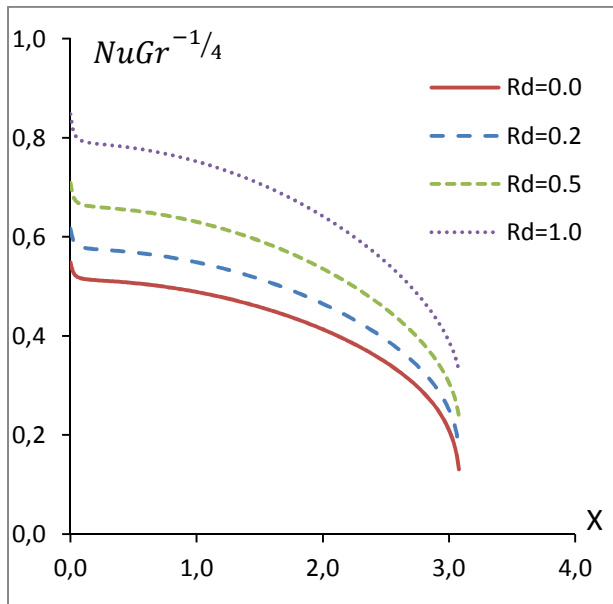


FIGURE 3. Local heat transfer or Nusselt number with $\gamma = 0.0$ and $Pr = 0.7$ at $t = 4.0$.

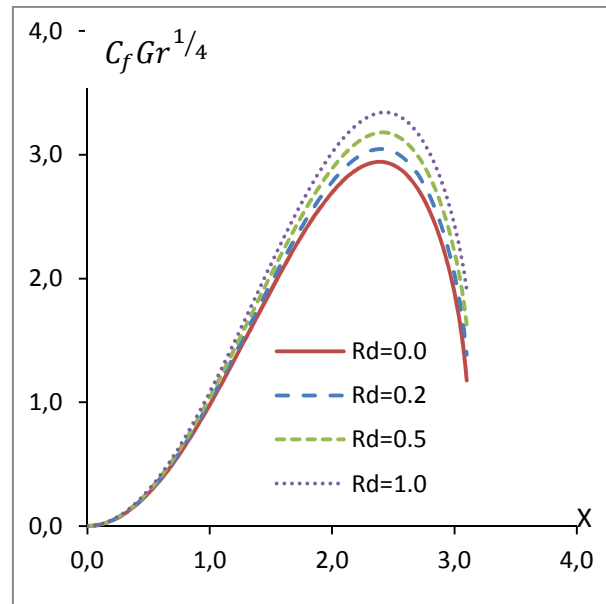


FIGURE 4. Local skin friction with $\gamma = 0.0$ and $Pr = 0.7$ at $t = 4.0$.

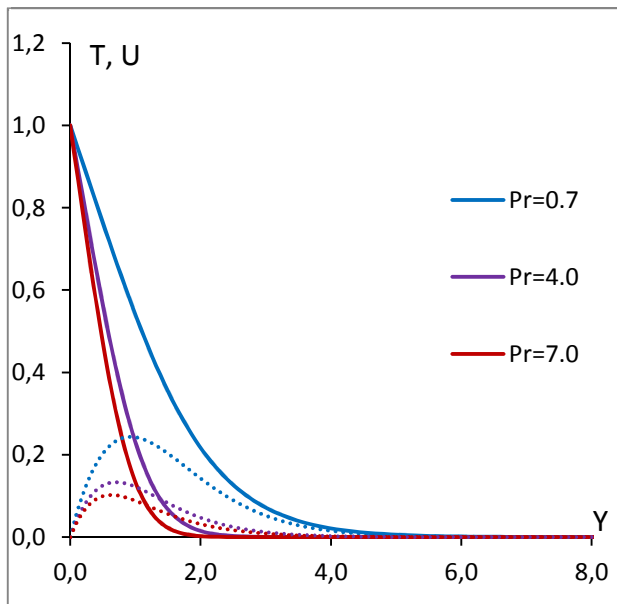


FIGURE 5. Temperature and velocity profiles against Y with $R_d = 0.2$ and $Pr = 0.7$ at $t = 4.0$ and $X = \pi/6$

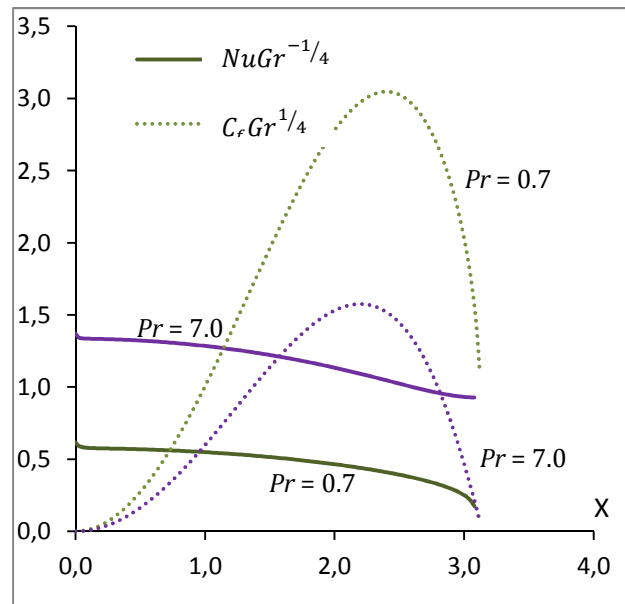


FIGURE 6. Local skin friction and Nusselt number with $\gamma = 0.0$ and $R_d = 0.2$ at $t = 4.0$ and $X = \pi/6$.

The variation of Pr on the velocity and temperature profiles when $R_d = 0.2$ at $t = 4.0$ are shown in the Figures 5. It is found that as the Pr increase, then both of the temperature and velocity decrease as well as the thermal boundary layer thickness decrease significantly. Variations of the local skin friction coefficient C_f and local Nusselt number Nu for different values of Pr while $R_d = 0.2$ at $t = 4.0$ are displayed in the Figures 6. From the figures, as Pr increase, the skin friction coefficient decrease and heat transfer coefficient increase.

CONCLUSION

The effect of radiation on natural convection flow on a heated horizontal cylinder has been investigated for different values of relevant physical parameters. From the results presented, the comparison between the present results and the previous study are found to be in good agreement. The results are also show an increase in the values of radiation parameter leads to increase in the velocity profile, the temperature profile, the local skin friction coefficient and the local rate of heat transfer. Besides that, the increase in Prandtl number leads to decrease in all the velocity profile, the temperature profile, the local skin friction coefficient but increase the local rate of heat transfer.

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