Performance of shape memory composite with SMA and SMP

H. Tobushi^{1, a}, S. Hayashi^{2, b}, Y. Sugimoto^{1, c} and K. Date^{1, d}

¹Department of Mechanical Engineering, Aichi Institute of Technology,
1247 Yachigusa, Yakusa-cho, Toyota, 470-0392, Japan.

²DiAPLEX Co., Ltd., Ebisu-minami 1-5-2, Shibuya-ku, Tokyo, 150-0022, Japan

^atobushi@aitech.ac.jp, ^bhayashi@diaplex.co.jp, ^cpp07711@aitech.ac.jp, ^dpp08715@aitech.ac.jp

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Abstract. The shape-memory composite belt with a TiNi-SMA wire fiber and a polyurethane-SMP sheet matrix was fabricated. The bending actuation characteristics of the belt were investigated by the thermomechanical tests. Residual deflection obtained by cooling under constant maximum deflection is close to the maximum deflection. The residual deflection disappears by heating under no load. Both the rates of shape fixity and shape recovery are close to 100%. Recovery force which appears by heating under constant residual deflection is 93-94% of the maximum force. The model of bending-spring constant of the shape-memory composite belt is proposed and evaluated based on the experimental data.

Introduction

Shape memory materials (SMMs) have been developed as smart materials. In SMMs, shape memory alloy (SMA) and shape memory polymer (SMP) have been used in practical applications^[1]. The shape memory effect (SME), superelasticity (SE) and large recovery stress appear in SMA^{[2],[3]}. However, both elastic modulus and yield stress are low at low temperature. This means the fact that rigidity of SMA elements is low at low temperature. The shape fixity (SF) and large shape recovery (SR) appear in SMP^{[4]-[6]}. However, both elastic modulus and yield stress are low at high temperature. This means the fact that rigidity of SMP elements is low at high temperature. If the shape memory composites (SMCs) with SMA and SMP are developed, new and higher functionality of the material can be obtained. That is, shape fixity and high rigidity at low temperature and shape recovery and recovery stress at high temperature can be used in the SMC. In the present paper, the characteristics of the SMC belt with SMA and SMP and the bending actuation properties were analysed. A TiNi SMA wire was used for the fiber of the SMC. A polyurethane (PU) SMP sheet was used for the matrix of the SMC. Since the fatigue life of TiNi SMA is very long, it has been most widely used in SMAs. Since PU SMP has various kinds of properties, it has been used in practical applications. The model of bending-spring constant of the SMC belt was proposed.

Characteristics of composite with SMA and SMP

The relationships between elastic modulus and temperature and those between yield stress and temperature for TiNi SMA, PU SMP and mild steel are schematically shown in Fig. 1. As it can be seen, the dependence of elastic modulus and yield stress on temperature is quite different among SMA, SMP and steel. In order to obtain the two-way shape memory effect (TWSME), two-way movement of SMA elements, the combination of SMA and bias materials, for example, steel is used in practical applications^{[1]-[3]}. If the composite materials with these materials are developed, new properties can be achieved. For example, if SMA and SMP are combined, the composite material with large recovery strain, high recovery stress, high rigidity, TWSME and light weight can be obtained. Therefore, if the SMCs with SMA and SMP are developed, new and higher functionality of the material can be expected.

Fig. 1 Dependence of elastic modulus and yield stress on temperature

Materials and Specimen

Polyurethane SMP (Diary MP5510 produced by Mitsubishi Heavy Industries, Ltd.) was used as the matrix of the SMC belt. The glass transition temperature of the SMP sheet T_g was 328K. A TiNi SMA wire (produced by Furukawa Electric Co.) was used for the fibers in the SMC. Diameter and length of the wire were 0.75mm and 50mm, respectively. The finish temperature of reverse transformation A_f of the wire was 325K. The SMC belt was fabricated as follows. First the lower half of the SMP sheet with thickness of 2.1mm was molded by mixing two kinds of liquid in a block. In a few minutes after molding, viscosity of the SMP became high enough to support the SMA wire on the surface of the SMP sheet. SMA wires were put on the lower half of the SMP sheet. The upper half of SMP was molded again on them. The SMC sheet was obtained by curing. Specimens of the SMC belt were cut from the SMC sheet into width of 10mm. The photograph of a specimen is shown in Fig. 2. As can be seen, the SMA wire was located in the central part of the SMC belt. Width, thickness and length of the SMC-belt specimen were 10mm, 4.2mm and 60mm, respectively.

Fig. 2 Photograph of specimen

Evaluation of Elastic Modulus and Spring Constant

If a concentrated force W is applied at the center of a simply supported beam, the maximum deflection y is expressed by the following equation

$$y = \frac{Wl^3}{48EI} \quad (1)$$

where E , I and l denote elastic modulus, second moment of area and distance between two supports. The relationship between W and y is expressed by using the bending-spring constant k as follows

$$W = k \cdot y \quad (2)$$

In the case of a SMA wire of diameter d , by using second moment of area $I_a = \pi d^4/64$, the bending-spring constant k_a is given

$$k_a = \frac{3\pi}{4l^3} E_a \cdot d^4 \quad (3)$$

where E_a denotes elastic modulus of the SMA.

In the case of a SMP beam of a rectangular cross section with width b and height t , by using second moment of area $I_p = bt^3/12$, the bending-spring constant k_p is expressed by the following equation

$$k_p = \frac{4}{l^3} E_p \cdot bt^3 \quad (4)$$

where E_p represents elastic modulus of the SMP.

In the present study, since the volume fraction of the SMA wire in the SMC belt is 1.05%, the bending-spring constant of the SMC belt k_c can be evaluated by a sum of k_a and k_p as follows

$$k_c = k_a + k_p = \frac{1}{l^3} \left(\frac{3}{4} \pi E_a d^4 + 4 E_p b t^3 \right) \quad (5)$$

With respect to the SMC belt, the bending-spring constant k_c is obtained from a slope of the initial loading curve by using Eq. (2). The SMC belt has a rectangular cross section of width b and height t . Therefore, elastic modulus in bending of the SMC belt E_c is given by the following equation

$$E_c = \frac{k_c}{4b} \left(\frac{l}{t} \right)^3 \quad (6)$$

The experimental and calculated results of k_c and E_c are shown in Table 1. As it can be seen, the bending-spring constant k_c and elastic modulus E_c of the SMC belt can be evaluated by the proposed model. The value of elastic modulus of the SMC belt E_c at T_g+30K is 48MPa which is larger than that for SMP $E_p=30MPa$ at T_g+30K . This means the fact that higher rigidity of SMC elements than one of SMP elements can be obtained in practical applications. As it can be found from Eq. (5), the rigidity of the SMC belt depends strongly on diameter of the SMA fiber and height of the SMP beam.

Table1 Values of elastic modulus and spring constant

Temperature	Experimental value			Calculated value			
	E_p [MPa]	E_a [GPa]	k_c [N/m]	k_p [N/m]	k_a [N/m]	k_c [N/m]	E_c [MPa]
T_g-25K	1150	20	55500	53250	233	53483	1155
T_g+30K	30	70	2240	1389	815	2204	48

Shape Fixity and Shape Recovery

The relationship between force and deflection and that between deflection and temperature obtained from the shape fixity and recovery test by the three-point bending with span $l=40mm$ are shown in Fig.3.

As it can be seen (Fig. 3a), the maximum force appears at deflection of $y_{max}=10mm$ in the loading process at T_g+30K ①. Force decreases almost to zero during the cooling process ② under constant y_{max} . As it can be seen in Fig. 3(b), deflection decreases at temperatures in the vicinity of A_f and T_g during the heating process ④ and approaches to zero at T_g+30K .

Fig. 3 Results obtained from shape fixity and recovery test by the three-point bending

Table2 Values of shape fixity and shape recovery rates

	Shape fixity rate R_f [%]	Shape recovery rate R_r [%]
Specimen 1	98.7	98.8
Specimen 2	99.7	99.6

The rate of shape fixity R_f and the rate of shape recovery R_r are defined by the following equations, respectively

$$R_f = \frac{y_u}{y_{\max}} \quad (7)$$

$$R_r = \frac{y_{\max} - y_h}{y_{\max}} \quad (8)$$

where y_u and y_h represent the deflection after unloading at T_g-30K and the deflection after heating up to T_g+30K , respectively. The values of the rate of shape fixity R_f and the rate of shape recovery R_r are shown in Table 2. It can be seen that both R_f and R_r are close to 100%, proving the excellent characteristics of shape fixity and shape recovery. The difference of shape fixity and shape recovery between two specimens is small.

Recovery Force

The relationship between force and deflection and that between force and temperature obtained from the recovery force test by the three-point bending with span $l=40mm$ are shown in Fig. 4.

As it can be seen in Fig. 4(a), the force-deflection curves during the loading ① and cooling ② are almost the same as those for the shape fixity and recovery test ② observed in Fig. 3. Recovery force increases during the heating ④ under constant $y_{\max}$.

As it can be seen in Fig. 4(b), force decreases almost to zero during the cooling ②. In the heating ④, force increases significantly at temperatures in the vicinity of A_f and T_g . The value of maximum recovery force obtained by heating up to T_g+30K is close to the maximum force given in the loading ①. The values of recovery force obtained during heating up to T_g+30K and the rate of recovery force to the maximum force during the loading ① are shown in Table 3. The rate of recovery force is 93-94%. The value of recovery force is higher than 7N which was obtained in the SMP belt without the SMA wire. Therefore, high recovery force can be obtained by SMC elements. The recovery force of SMC elements depends on the volume fraction and the arrangement of SMA fibers.

The development of SMC elements with high functionality is expected by various combinations of SMAs and SMPs. That is, if A_f of SMA is higher than T_g of SMP, the two-way property can be used during heating and cooling.

Fig. 4 Results obtained from recovery force test by the three-point bending

Table3 Values of maximum force, recovery force and the rate of recovery force to maximum force

	Maximum force [N]	Recovery force [N]	Rate of recovery force [%]
Specimen 1	11.6	10.9	93.2
Specimen 2	13.6	12.8	94.3

CONCLUSION

The SMC belt was fabricated by combining the TiNi-SMA wire fiber and the polyurethane-SMP sheet matrix. The bending actuation characteristics of the SMC belt were investigated. The results obtained can be summarized as follows.

- (1) Although spring constant of the SMC belt for bending is large at low temperature, it is small at high temperature. The spring constant of the SMC belt can be evaluated by the proposed model with simple combination of the SMA wire and the SMP sheet.
- (2) Force decreases on cooling under constant maximum deflection and high residual deflection close to the maximum deflection is obtained. The residual deflection disappears on heating under no load. The rates of shape fixity and shape recovery close to 100% can be obtained.
- (3) The recovery force which appears on heating under constant residual deflection is 93-94% of the maximum force given in the loading process at T_g+30K .

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